

# The factorization of the $q$ -difference operators

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We present certain classes of second order  $q$ -difference operators, which admit factorization into first order operators acting in a Hilbert space. Solutions of the  $q$ -deformed Schrödinger equation are presented for the following potentials: shifted oscillator, isotropic oscillator, Morse potentials. We also discuss classical limit case by letting  $q \rightarrow 1$ .

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